TutorTube: Factoring 101 Fall 2019

Introduction

Hello and welcome to TutorTube, where The Learning Center’s Lead Tutors help you understand challenging course concepts with easy to understand videos. My name is Haley Higginbotham, Lead Tutor for Math. In today’s video, we will explore factoring. Let’s get started!

Factoring 101

Factoring is a very useful skill when you want to either solve for the roots of an equation, or just solve for . In most math classes, factoring is used on quadratics, which have the form where are constants. Let's take a look at the different ways to factor.

Tree Method

To explain the tree method, I think it's best that we take a look at an example.

Example:

Now, let's set up our tree. Generally, it is going to look like this:

c

b

+

=

In our case, and . So, we need something that will multiply to give us , and add to give us .

2

-3

+

=

Well, the only factors (numbers that multiply) to give us are and . However, gives us , not . To fix this, let's make both numbers negative, since . Now , which is what we want.

2

-1

-2

-3

+

=

Therefore, our factored form of is . To check if this is correct, we could multiply the two factors back together by distributing (more commonly referred to as FOILing). Multiplying back out gives us which simplifies to .

Practice:

Factor the following completely.

1.

2.

3.

Important Note: To use the Tree Method, your value needs to be equal to (). Recall that the value is the number in front of the .

Greatest Common Factor (GCF)

Now let's look at another method, Greatest Common Factor, or GCF for short. To factor by the GCF, you need to take out the biggest term that all the terms have.

Example:

Let's start by taking a look at just the numbers, , , and . What is the greatest factor they have in common? If you said , that is correct! So now we know that is part of our GCF. Now let's look at the variables, , , . The GCF here would be , since it goes into both and .

So, our GCF in this case is . By factoring out from each term, we get:

Now we can use the Tree Method to simplify even further, and we get

as our fully factored answer.

Practice:

Factor the following completely.

4.

5.

6.



Note: GCF is usually used in combination with one of the other methods for factoring.

Difference of Two Squares (DOTS)

Difference of Two Squares (DOTS) is more of a shortcut. You can still factor without knowing DOTS using the Tree Method, this is just a quicker way to do it. You'll know you can use DOTS if it has the form . If it has this form, the factors will be .

Example:

This can be rewritten as . Therefore, our factors are . We can verify this is true by distributing back out, but I'll leave that up to you if you wish to see.

Practice:

Factor the following completely.

7.

8.

9.

By Grouping

To factor by grouping, we are also going to need GCF. We want to group terms together that have the GCF.

Example:

Let's go ahead and group as follows: , with as the GCF for the first group, and as the GCF for the second group. It'll be clear why I took to be the GCF in a minute.

After factoring out the GCFs, we have

You might notice that there is a next to the GCFs. That actually becomes the new GCF of and . If it helps, think of as a variable, let's say . Then we would have . Now, it's a little clearer that we have as the GCF. So, if we factor out the new GCF, we have

And since we said , we can plug it back in to get

which is the final factored form of .

Now, as for why I took out as opposed to . If you take out a , you end up with

and you'll get stuck since unless you see you're also supposed to take out the negative. However, if you forget, it's okay, since you can just take the negative out at this step in order to make them the same.

Practice:

Factor the following completely.

10.

11.

12.

Note: Sometimes, you'll have to move terms around in order to get the best combination of GCFs. It's alright to try a couple different ones! Typically, the best ones to group are the ones that have the most powers of in common.

AC Method

Recall that the standard form of a quadratic is , where are constants. If you refer back to the Tree Method, you'll notice I made a note about how it only works if . The AC Method deals with when and combines the Tree Method and Grouping Method.

Example:

In this example, our value is , which means we can't use just the Tree Method. There's not a GCF for all three constants, and it's not a Difference of Two Squares. And it's not easy to see how things should be grouped, if they can be at all. So, that leads us to the AC Method.

It's the same idea as the Tree Method to start, except we have to make sure we multiply and use as opposed to just . Generally, we want this:

ac

b

+

=

In this case, so that goes in the top box. And , so that goes in the far right box.

24

-10

+

=

Similar to before, we need factors of that add to give us .

Factors of include:

|  |  |
| --- | --- |
|  |  |
|  |  |
|  |  |
|  |  |

The only factors that give us are and .

24

-4

-6

-10

+

=

So, instead of directly giving us the factors like in the Tree Method, it actually breaks up the value so we can use grouping.

Now, we can group like we typically would.

Practice:

Factor the following completely.

13.

14.

15.

Answers to Practice Problems:

1.

2.

3.

4. , GCF of

5. , GCF of

6. No GCF, already in simplest form

7.

8.

9. DOTS does not apply here since we are not subtracting (**Difference** of Two Squares, not Addition of Two Squares). Therefore, this is actually not factorable in the real numbers.

10.

11.

12. . Note that sometimes the GCF is , which is fine.

13.

14.

15.

Outro

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